On network analysis and user behavior

Ramayya Krishnan iLab, The H. John Heinz III College Carnegie Mellon University Pittsburgh, PA rk2x@cmu.edu

Outline

- Two examples
 - Intra-organizational KM the role of triadic closure or cliques in determining user behavior
 - Product adoption the role of social influence vs.
 homophily
- Key points
 - Multi-disciplinary perspective that blends computational and social science is needed
 - New estimation methods to work with novel data sets
 - Need for new methods to design and conduct experiments in a networked world

Example 1: Social Media and Knowledge Management in a Global Organization

Sample data posting of query and responses

threadid	associateid	postedtime	messagetype	subject	message
{20070110-	138242	2007-01-10 06:41:15	Query	Panel Creation in REXX	Hi,
{20070110-	122971	2007-01-10 07:42:54	Response	Re: Panel Creation in REXX	For retaining the input panel
{20070110-	107246	2007-01-10 13:20:24	Response	Re: Panel Creation in REXX	You are not creating the
{20070110-	128623	2007-01-17 07:19:18	Response	Re: Panel Creation in REXX	No need to VPUT you can
{20070110-	129498	2007-03-01 12:31:42	Response	Re: Panel Creation in REXX	it's simple if var1 var2 are the
{20070110-	107246	2007-03-01 13:49:16	Response	Re: Panel Creation in REXX	TYPE(INPUT) is to define the
{20070110-	125034	2007-04-14 07:17:32	Response	Re: Panel Creation in REXX	You can use the command
{20070110-	107246	2007-04-14 23:43:30	Response	Re: Panel Creation in REXX	ADDRESS
	0000000				

Sample Query

- Query on: Singleton class and threads in Java
- Responses:
- 1. Singleton class means that any given time only one instance of the class is present, in one JVM. So, it is present at JVM level.
- The thing is if two users(on two different machines which has separate JVMs) are requesting for singleton class then both can get one-one instance of that class in their JVM.

Data description

- Message level and thread-level data from forum
- Message characteristics
 - Posting time, EmployeeID, Thread, Type of message (query or response), content of message etc.
- User characteristics
 - EmployeeID, Tenure at firm, Age, Gender, Location, Division, Job Title

Network structure evolution

Sequence of Actions:

- User 301 posts a query Q1000
- Users 502, 641 post responses
- User 900 posts a query Q1001
- Users 301, 641 post responses



Network structure

Asymmetric tie:

 A as responded to B's query but B has not responded to A

Sole-symmetric tie:

 Users have responded to each other, but not as part of a clique

Simmelian Tie:

 Users are part of a 'clique', whose members have all responded to one another

Simmelian Ties

Research Questions

- Can Simmelian ties be established in an electronic communications medium with repeated interactions? Will they matter?
- 2. Do these ties depend upon the context? Do more instrumental contexts result in weaker Simmelian ties or less effective Simmelian ties?
- 3. Do both current context (what type of query) or past context in which the tie was established matter?

Dependent variable:

Number of response by A to B in period two



Dependent variable:

Number of response by A to B in period two

Explanatory Variables:



Dependent variable:

Number of response by A to B in period two

Explanatory Variables:



Dependent variable:

Number of response by A to B in period two

Explanatory Variables:



Dependent variable:

Number of response by A to B in period two

Explanatory Variables:



Dependent variable:

Number of response by A to B in period two

Explanatory Variables:



Example 2: Social Influence vs. Homophily in product/service adoption

• Focus on identifying users that can help diffuse "information" over the network

 Learn about the power of "social influence" as trigger for the diffusion process

 Learn about how social influence is associated to "contagious churn"

Research Question

Can we predict consumers' product purchase decisions...

➢ Using social network information?

Theoretical Foundation

➢ Homophily (Mcpherson et al. 2001)

➤ "Birds of a feather flock together"



The Challenge

➢ Large-scale network





Literature

A rich literature on networks from various fields (e.g. Kleinberg 1999, Brin and Page 1998)

Network-based marketing

Network Neighbors: Hill, Provost, Volinsky (2006)
 Viral Marketing: Richardson and Domingos (2002)

Classification: Macskassy and Provost (2003, 2007)

> What about *unobserved product taste*?

> For small, tightly connected groups: Hartmann (2010)

But what about large-scale networks of arbitrary connection structure?

This Study

- Model correlated purchase behaviors of consumers in a large social network...
- Using Gaussian Markov Random Field (GMRF) to characterize latent product taste
 - Handle networks of arbitrary topology
 - Encapsulate conditional independence
- Estimation result confirms the positive taste correlation among connected people
- Predictive performance better than existing LR based models, and better than SVM based models, too.

Data

Obtained from a large Asian telecom company

- ➤ 231,416 customers
- ≻6 month period
- Detailed phone call data
 - ≻Who called whom, when
- > Demographics information: gender, age
- > Purchase records of caller ringback tone (CRBT)
 - ➤Who purchased what, when

> Can we predict CRBT adoption decisions?

Descriptive Statistics

	Mean	SD	Min	Max
Gender	Male	218017	Female	13399
Age	40.56	13.67		
Number of Consumers Called by Each Consumer	13.73	22.9	1	2858
Number of Phone Calls Per Consumer	410.4	942.7	1	59016
		Adoption		
	Number	Percentage		
Number of Consumers	231416			
Number of Consumers Who Adopted CRBT	79505	34.36%		
Adoption Percentage by Gender	Male	34.50%	Female	31.89%

Preliminary analysis: gender doesn't help much in prediction...

Data – Preliminary Analysis

Age doesn't help much, either...



Data – Preliminary Analysis

Node degree helps a lot (need for social network)!



Data – Preliminary Analysis



Maybe, but need the discipline of a model

Model

There are *I* consumers in a social network

Connection matrix: $C = [c_{ij}]$

$$c_{ij} = \begin{cases} 1 & \text{if consumers } i \text{ and } j \text{ are connected} \\ 0 & \text{otherwise} \end{cases}$$

Adoption decision: $D_i = \begin{cases} 1 & \text{if consumers } i \text{ adopts the product} \\ 0 & \text{otherwise} \end{cases}$

Adoption Probability

Binary Probit Model

 $Pr(D_i = 1) = Pr(U_i >= 0)$

$$U_i = \alpha_i + \beta X_i + \varepsilon_i$$

$$\varepsilon_i \sim N(0,1)$$
 Random disturbance

- *X_i* Observed individual characteristic (gender, age, connection degree)
- α_i Unobserved product taste Modeled as a GMRF!

Gaussian Markov Random Field (GMRF)

Definition (GMRF): A random vector $\vec{x} = (x_1, ..., x_n)^T$ is called GMRF w.r.t. the undirected graph $G = (V = \{1..n\}, E)$ with mean $\bar{\mu}$ and precision matrix Q > 0 if and only if its density has the form:

$$\pi(\vec{x}) = (2\pi)^{-n/2} |Q|^{1/2} \exp(-\frac{1}{2}(\vec{x} - \vec{\mu})^T Q(\vec{x} - \vec{\mu}))$$

And

 $Q_{ij} \neq 0 \Leftrightarrow \{i, j\} \in E, \forall i, j$

► A multivariate normal vector

Connection structure encoded in its precision matrix

Non-zero off-diagonal elements correspond to connections

Properties of GMRF

Can model connections of arbitrary topology

➢ Better than using in-group correlation

> Encodes conditional independence



Consumers 1 and 3 should be correlated But conditional on consumer 2, they should be independent

> Model parameters have intuitive explanations

Model Latent Product Taste Using GMRF

$$\begin{pmatrix} \alpha_1 \\ \dots \\ \alpha_I \end{pmatrix} \sim N(\begin{pmatrix} \overline{\alpha} \\ \dots \\ \overline{\alpha} \end{pmatrix}, Q^{-1})$$

$$Q = [q_{ij}]$$
, where $q_{ij} = 0$ if $c_{ij} = 0$

Straightforward Interpretation :

Precision
$$(\alpha_i | \alpha_{-i}) = q_{ii}$$

 $\operatorname{Cor}(\alpha_i, \alpha_j | \alpha_{-ij}) = -q_{ij} / \sqrt{q_{ii}q_{jj}}$

Parameterization (base model, model B):

$$Q = \begin{pmatrix} \kappa & -r\kappa & 0 & \dots & -r\kappa \\ -r\kappa & \kappa & 0 & \dots & 0 \\ 0 & 0 & \kappa & \dots & -r\kappa \\ \dots & \dots & \ddots & \dots \\ -r\kappa & 0 & -r\kappa & \dots & \kappa \end{pmatrix}$$

- *r* Conditional correlation between connected consumers
- κ Conditional precision

Model Extension

Model AI:

1

$$Q^{I} = \begin{pmatrix} \kappa_{d_{1}} & -r\sqrt{\kappa_{d_{1}}\kappa_{d_{2}}} & 0 & \dots & -r\sqrt{\kappa_{d_{1}}\kappa_{d_{1}}} \\ -r\sqrt{\kappa_{d_{1}}\kappa_{d_{2}}} & \kappa_{d_{2}} & 0 & \dots & 0 \\ 0 & 0 & \kappa_{d_{3}} & \dots & -r\sqrt{\kappa_{d_{3}}\kappa_{d_{1}}} \\ \dots & \dots & \dots & \ddots & \dots \\ -r\sqrt{\kappa_{d_{1}}\kappa_{d_{1}}} & 0 & -r\sqrt{\kappa_{d_{3}}\kappa_{d_{1}}} & \dots & \kappa_{d_{1}} \end{pmatrix} \qquad \kappa_{d} = \kappa_{0} + \kappa_{1} \cdot \log(d+1)$$

The more we know about a consumer's connections, the more we should know about the consumer

Model All:

$$Q^{II} = \begin{pmatrix} \kappa_{d_1} & -r_{21}\sqrt{\kappa_{d_1}\kappa_{d_2}} & 0 & \dots & -r_{I1}\sqrt{\kappa_{d_1}\kappa_{d_1}} \\ -r_{21}\sqrt{\kappa_{d_1}\kappa_{d_2}} & \kappa_{d_2} & 0 & \dots & 0 \\ 0 & 0 & \kappa_{d_3} & \dots & -r_{I3}\sqrt{\kappa_{d_3}\kappa_{d_1}} \\ \dots & \dots & \dots & \ddots & \dots \\ -r_{I1}\sqrt{\kappa_{d_1}\kappa_{d_1}} & 0 & -r_{I3}\sqrt{\kappa_{d_3}\kappa_{d_1}} & \dots & \kappa_{d_I} \end{pmatrix} r_{ij} = r_0 + r_1 \cdot \log(Call_{ij})$$

The more communication between two consumers, the stronger the tie should be, and the stronger the correlation

Estimation

Hierarchical Bayesian approach

>MCMC draws with hybrid Metropolis-Gibbs fashion

$$f(\alpha_i \mid \alpha_{-i}, \beta, \alpha, r, \kappa, X_i, D_i, C) \propto \varphi(\alpha_i \mid \alpha_{N(i)}, \alpha, r, \kappa) L(D_i \mid \alpha_i, \beta, X_i, D_i)$$

$$f(\overline{\alpha} \mid \alpha_i : i = 1..I) \propto \phi((I + V_{\alpha})^{-1} (\sum_{i=1}^{I} \alpha_i + V_{\alpha} \overline{\alpha}), (I + V_{\alpha})^{-1})$$

$$f(\beta \mid \alpha_i : i = 1..I, X_i, D_i) \propto \pi(\beta) \prod_{i=1}^{I} L(D_i \mid \alpha_i, \beta, X_i, D_i)$$

$$f(r \mid \alpha_i : i = 1..I, \beta, \overline{\alpha}, \kappa, C) \propto \pi(r) \prod_{i=1}^{I} \varphi(\alpha_i \mid \alpha_{N(i)}, \overline{\alpha}, r, \kappa)$$

$$f(\kappa \mid \alpha_i : i = 1..I, \beta, \overline{\alpha}, r, C) \propto \pi(\kappa) \prod_{i=1}^{I} \varphi(\alpha_i \mid \alpha_{N(i)}, \overline{\alpha}, r, \kappa)$$

Identifying Connections

- Based on phone call data
- Using a "threshold" method: two consumers are considered as connected if they made at least a certain number of phone calls
- Endogenizing network formation left for future extension

> Vary threshold value to ensure robustness

Dividing Training and Testing Data



- >80% of consumers for training, 20% for testing
- ➢ Each node (consumer) is individually randomly assigned ("flip-a-coin") to training or testing set.
- ➤The sub-network consisting of training nodes is used for estimation
- Other division methods possible, for future extension
 Vary training dataset size for sobustness check

Result: Parameter Estimation

Model B



>The higher the threshold value, the higher the correlation

➢Higher threshold filter out more "noise"

Result: Parameter Estimation

Model AI

Threshold	κ	0	κ_{1}	!	r		
1111001010	Mean	SD	Mean	SD	Mean	SD	
1	0.129	0.0011	-0.013	0.00031	0.0227	0.00038	
3	0.115	0.00093	-0.0097	0.00037	0.03487	0.0006	
5	0.113	0.00153	-0.0094	0.00061	0.03912	0.00079	
8	0.108	0.0011	-0.008	0.00075	0.0469	0.00088	
10	0.1043	0.0015	-0.0063	0.00084	0.0536	0.00094	
20	0.101	0.0016	-0.0054	0.00091	0.0607	0.0012	
)			

Conditional precision is lower for nodes with higher degree

➢ Possibly explained by heterogeneity

Result: Parameter Estimation

Model All

Threshold	κ	0	κ	1	r	0	r	<i>r</i> ₁		
	Mean	SD	Mean	SD	Mean	SD	Mean	SD		
1	0.129	0.0011	-0.0127	0.0004	-0.0013	0.000832	0.0128	0.0004		
3	0.117	0.0008	-0.0099	0.0004	-0.021	0.0022	0.0183	0.0007		
5	0.11	0.0012	-0.0078	0.0006	-0.025	0.0034	0.0199	0.001		
8	0.1077	0.0016	-0.0074	0.0008	-0.0476	0.0035	0.0253	0.0009		
10	0.1051	0.0011	-0.0063	0.0006	-0.0444	0.0047	0.0242	0.0012		
20	0.0994	0.0014	-0.004	0.00087	-0.056	0.0061	0.0283	0.0014		

➤The more frequently the communication, the higher the conditional correlation!

➢Not all connections are the same; strength matters.

Predictive Performance

➢ Prediction Approach:

➤"Individual-based": predict adoption when calculated probability is 0.5 or higher.

➤ "Top-k": predict adoption for the k consumers with the highest calculated probabilities.

➤ Evaluation Approach:

>Accuracy: percentage of correct predictions

Precision: percentage of correct predictions when the prediction is to adopt

Benchmark Models

Model	Explanatory Variables	Mechanism
BM1	Gender, Age	Logistic Regression
BM2	Gender, Age, Degree	Logistic Regression
BM3	Gender, Age, Degree, Percentage of Neighbors who Adopt	Logistic Regression
	Gender, Age, Degree, Percentage of	Suppor Vector Machine,
BM4	Neighbors who Adopt	Linear Kernel
	Gender, Age, Degree, Percentage of	Suppor Vector Machine,
BM5	Neighbors who Adopt	Polynomial Kernel

Accuracy – Individual Based

					Percent of Correct Prediction						
	Total Test	Total	A	doption						"Naive"	
Threshold	Cases	Adoption	Pe	ercent	M	ode B	Model AI	N	lodel AII	М	odel
1	46092	15752		34.18%		66.82%	66.71%		67.14%		65.82%
3	42675	15205		35.63%		65.93%	66.10%		66.52%		64.37%
5	39575	14234		35.97%		65.35%	65.24%		66.06%		64.03%
8	36715	13674		37.24%		64.52%	64.97%		65.49%		62.76%
10	35290	13103		37.13%		64.38%	63.84%		64.79%		62.87%
20	29846	11520		38.60%		63.11%	63.20%		63.74%		61.40%
ND attar tha		adal (nati	ل م	(much)				1			
F Beller Ina	n naive mo	bael (not i	by	much) -							
➤Higher thr	eshold lead	ds to lowe	er	accurac	y -						
Dut that's baseuss "the problem gets barder"											
📕 Dut tildt S	necause i	ine proble	211	i gets na	11(

Precision – Individual Based

		Mod	el B	Mode	elAI	Model AII		
	Predicted		Correct	Predicted	Correct	Predicted	Correct	
Threshold Ado		Adoption	Percentage	Adoption	Percentage	Adoption	Percentage	
	1	8385	52.88%	7671	52.76%	8129	53.72%	
	3	5658	55.07%	6439	55.71%	6752	56.80%	
	5	6609	54.18%	6359	55.56%	6672	56.01%	
	8	6707	54.96%	6333	55.35%	6700	57.48%	
	10	6182	55.26%	7 344	54.10%	6242	55.43%	
	20	6213	54.45%	5977	55.19%	6693	55.22%	

Much better than naïve model

≻Model All is the best

➢Performance best at medium threshold

➢Balance between filtering out noise and retaining information

Benchmark Precision – Individual Based

	Mode	Model BM2			Model BM3			
	Predicted	Correct	Pr	redicted	(Correct		
Threshold	Adoption	Percentage	A	deption	Pe	rcentage		
1	2006	56.23%		2089		59.89%		
3	2060	54.13%		2226		57.77%		 Slightly higher procision
5	4142	56.78%		1951		58.89%		Singlicity higher precision
8	5475	55.87%		2015	K	60.10%		On much fewer predictions
10	7124	52.91%		2176		59.93%		on machiewer predictions:
20	10939	48.43%		2289		62.69%		
					ノ)	

	Mod	el B	Mode	el AI	Model AII		
	Predicted	Correct	Predicted	Correct	Predicted	Correct	
Threshold	Adoption	Percentage	Adoption	Percentage	Adoption	Percentage	
1	8385	52.88%	7671	52.76%	8129	53.72%	
3	5658	55.07%	6439	55.71%	6752	56.80%	
5	6609	54.18%	6359	55.56%	6672	56.01%	
8	6707	54.96%	6333	55.35%	6700	57.48%	
10	6182	55.26%	7344	54.10%	6242	55.43%	
20	6213	54.45%	5977	55.19%	6693	55.22%	

Benchmark Precision – Individual Based

	Model	BM4		Model BM5			
	Predicted	Correct	Pred	icted	Correct		
Threshold	Adoption	Percentage	Ado	ption	Percentage		
1	3470	62.07%		1654	68.50%		
3	3718	61.97%		1946	65.83%		🔶 Same story here
5	3371	62.06%		2529	64.41%		• • • • • • • • • • • • • • •
8	4383	62.03%		2977	65.10%		
10	4712	60.36%		3474	63.27%		
20	4688	60.30%		3403	62.83%		
						/	

	Mod	el B	Mode	el AI	Model AII		
	Predicted Correct		Predicted	Correct	Predicted	Correct	
Threshold	Adoption	Percentage	Adoption	Percentage	Adoption	Percentage	
1	8385	52.88%	7671	52.76%	8129	53.72%	
3	5658	55.07%	6439	55.71%	6752	56.80%	
5	6609	54.18%	6359	55.56%	6672	56.01%	
8	6707	54.96%	6333	55.35%	6700	57.48%	
10	6182	55.26%	7344	54.10%	6242	55.43%	
20	6213	54.45%	5977	55.19%	6693	55.22%	

Precision – Top-K

	Mod	el B	Mode	el AI	Model AII		
Threshold	Top 1000	Top 2000	Top 1000	Top 2000	Top 1000	Top 2000	
1	66.00%	65.80%	65.90%	62.25%	66.30%	65.35%	
3	69.80%	64.60%	68.60%	64.90%	72.00%	68.00%	
5	69.80%	67.00%	69.60%	65.10%	73.10%	68.75%	
8	71.10%	67.05%	67.50%	64.65%	73.80%	68.55%	
10	71.40%	65.55%	68.70%	65.25%	71.70%	67.40%	
20	70.50%	66.40%	73.50%	66.90%	72.40%	67.10%	

>Much higher precision than individual-based predictions

➤Model All is still the best

>Almost twice the accuracy of a naïve model

➢Performance again the best for medium threshold values

Benchmark Precision – Top-K

	Model BM1		Model BM2		Model BM3	
Threshold	Top 1000	Top 2000	Top 1000	Top 2000	Top 1000	Top 2000
1	34.20%	34.05%	59.60%	56.25%	62.20%	60.25%
3	36.10%	35.90%	55.70%	53.90%	60.50%	57.90%
5	35.80%	35.80%	54.50%	52.45%	61.50%	59.00%
8	35.70%	37.75%	55.50%	53.90%	61.40%	60.00%
10	36.00%	38.70%	54.10%	53.25%	60.50%	59.45%
20	36.80%	38.15%	54.90%	52.15%	63.60%	62.85%

Logistic-regression based models not nearly as good

Benchmark Precision – Top-K

	Model	BM4	Model BM5		
Threshold	Top 1000	Top 2000	Top 1000	Top 2000	
1	68.10%	66.25%	71.10%	67.05%	
3	69.30%	65.25%	70.10%	65.90%	
5	70.50%	65.70%	71.80%	66.70%	
8	67.10%	66.80%	69.70%	67.50%	
10	68.80%	65.60%	70.40%	66.80%	
20	70.30%	68.25%	74.60%	67.40%	

SVM-based models almost as good, but still lower

In Pictures...



Varying Training Dataset Size

	Model AII			Model BM5		
TrainingPortion	Individual	Top 1000	Top 2000	Individual	Top 1000	Top 2000
90%	56.85%	69.40%	62.20%	64.55%	66.10%	61.55%
80%	56.17%	71.60%	68.05%	66.11%	73.70%	67.55%
70%	55.30%	73.10%	69.25%	65.03%	72.10%	68.60%
60%	54.83%	74.90%	70.30%	63.46%	71.80%	68.55%
50%	53.86%	74.60%	71.85%	63.14%	73.90%	69.55%
40%	54.32%	76.50%	73.80%	61.31%	74.20%	70.90%
30%	53.64%	73.60%	69.75%	61.74%	74.40%	70.35%
20%	52.86%	72.30%	69.70%	61.92%	72.80%	69.25%
10%	52.74%	69.70%	68.40%	56.17%	69.30%	64.80%

Result and comparison both stable

➢Precision has an "inverted-U" shape w.r.t. training data size

➢ Fewer good candidates when test dataset is smaller

Future Extensions

Dynamic Model

- Repeat purchase decisions
- Product choice decisions

Incorporate Influence
 We have communication data!

Endogenize network formation

Key take aways

Modeling the correlation of latent product tastes
 In a large-scale social network
 Using Gaussian Markov Random Field (GMRF)

- Estimation confirms positive correlation among connected consumers
 - We have communication data! Higher correlation for stronger ties
- Predictive precision better than logistic regression based and SVM based benchmark models









NGAPORE MANAGEMENT

INTVERSITY.



Launch of SMU-CMU LIVING ANALYTICS RESEARCH CENTRE 7 March 2011

ANALYSE, PREDICT

- Analyse Traces
- Understand Behavioural Patterns Over Time & Context
- Predict Behaviour



EXPERIMENTS

Changes to

- Attributes of products, services
 & experiences
- Individual level interaction & information
- Group & network level interaction
 - & information

OBSERVE



The "Digital Traces" of Behaviour and Living

HUMAN ACTION

Individual responses; group & network responses

LA RESEARCH AREAS

Area A: Intelligent Systems for Mining & Analytics

Dynamic Network Science

Adaptive Decision Analytics Area B: Social & Management Science

Understanding and Predicting Behaviour in Real-Time Context

Design of Guidance and Incentives for Influencing Behaviour Area D: Data Fusion & Privacy

> Data Privacy & Protection

Data Fusion & Record Linkage Area E: Systems & Infrastructure

> Basic Computing, Storage, & Network Infrastructure

Cloud Computing for Real-Time LA

Next-Gen Mobile Sensing and Analytics

Area C: Network Experimentation

Randomisation and optimal design in networked environments

Experiments with network data

 Statistical theory of design of experiments assumes independence between test and control

 This independence is violated in network settings since observations are affected by network interaction and influences

• This is work to be done and one of the key areas of focus of the Living Analytics Center