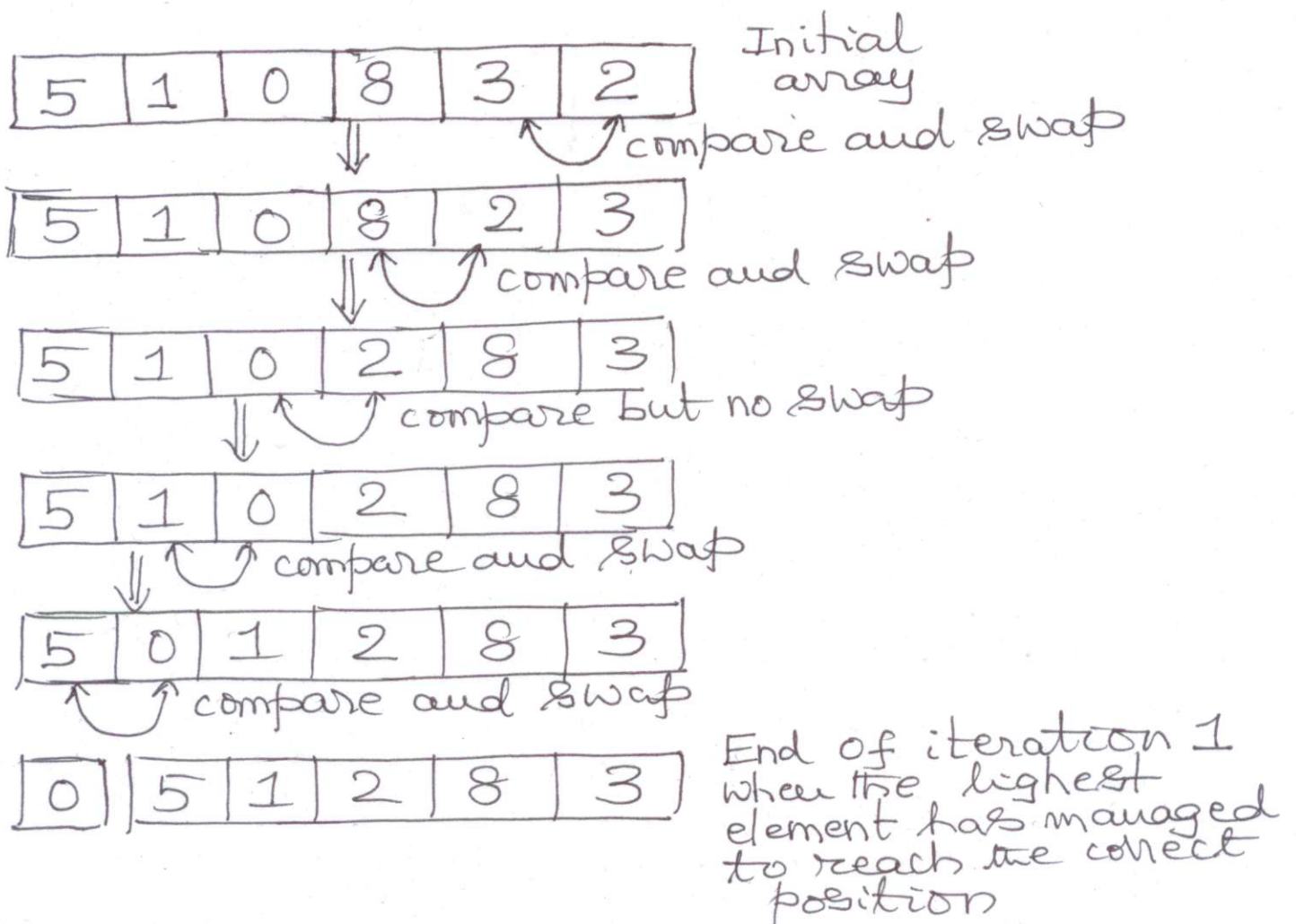
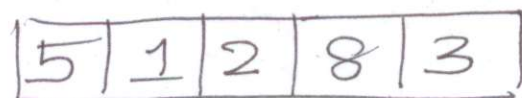


BUBBLE SORT

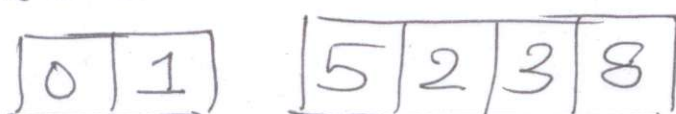
This method proceeds in $(n-1)$ iterations. In each iteration, the lightest (smallest) element of the unsorted portion of the array "bubbles" up to its "correct" position, through a series of comparisons and exchanges. An example follows.



In iteration 2, we repeat the above procedure with the unsorted portion



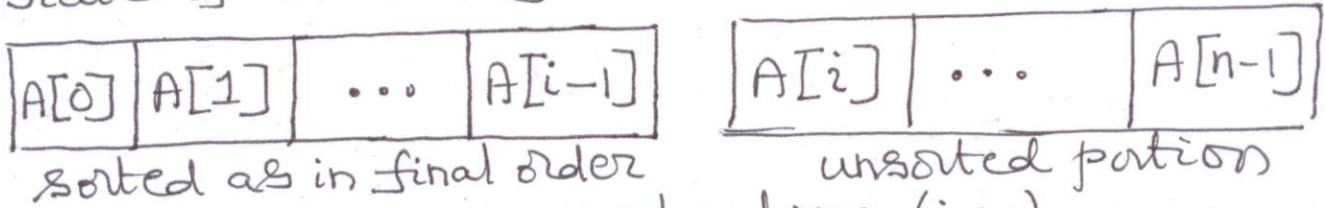
to obtain



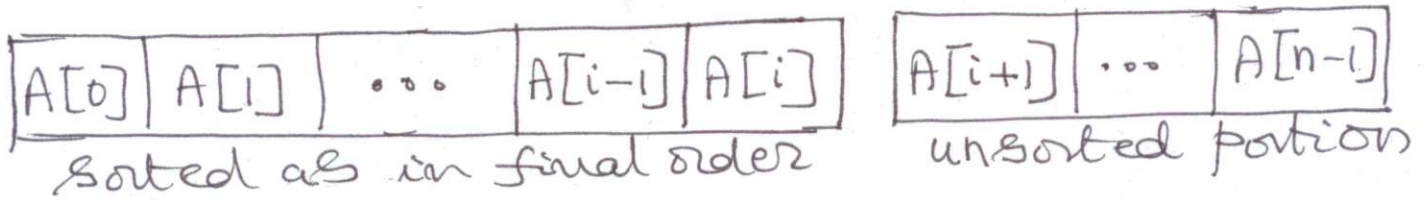
and this repeats.

Summary of Bubble Sort

state of the array at the end of Iteration "i"



|| Iteration (i+1)
 || The next lowest key from
 || unsorted portion bubbles up
 || and becomes $A[i]$

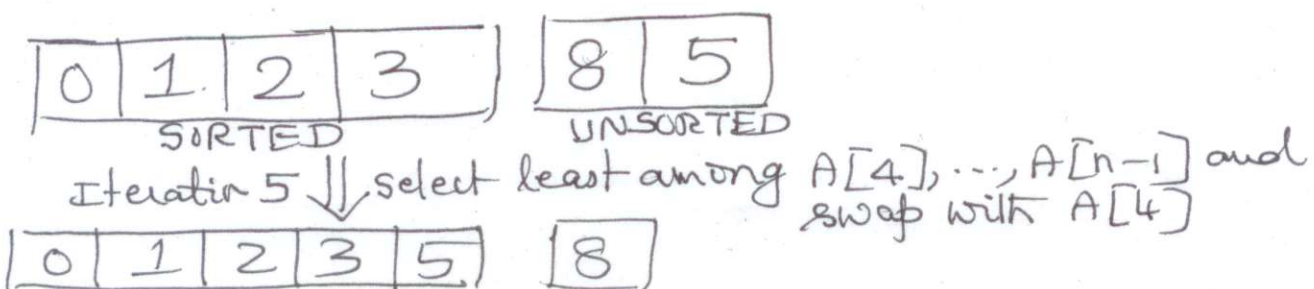
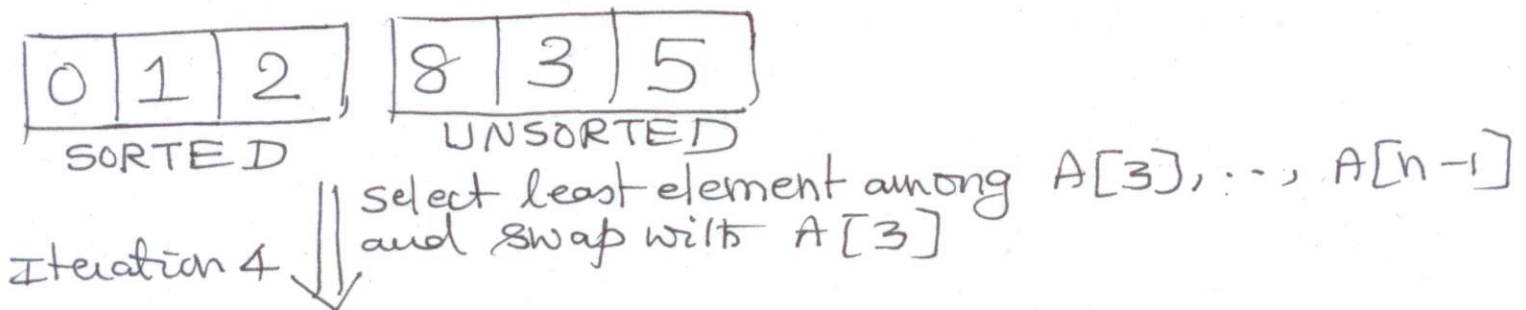
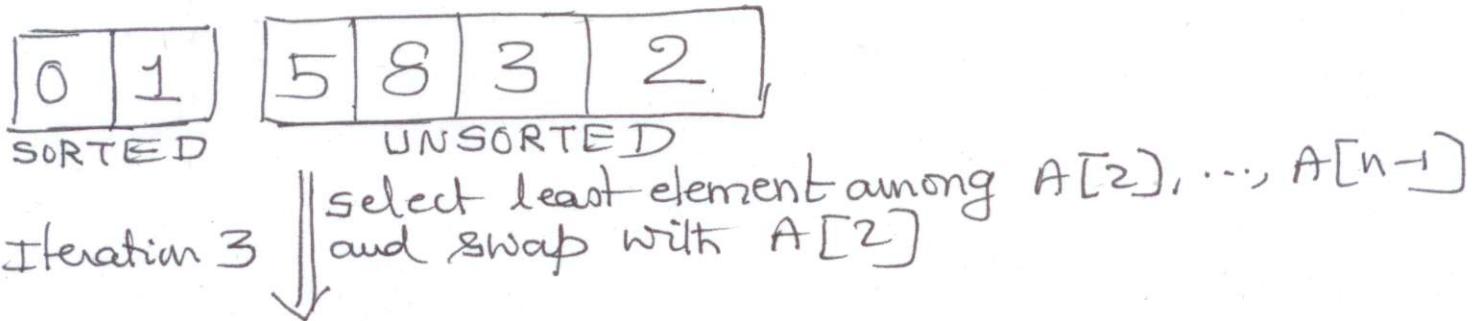
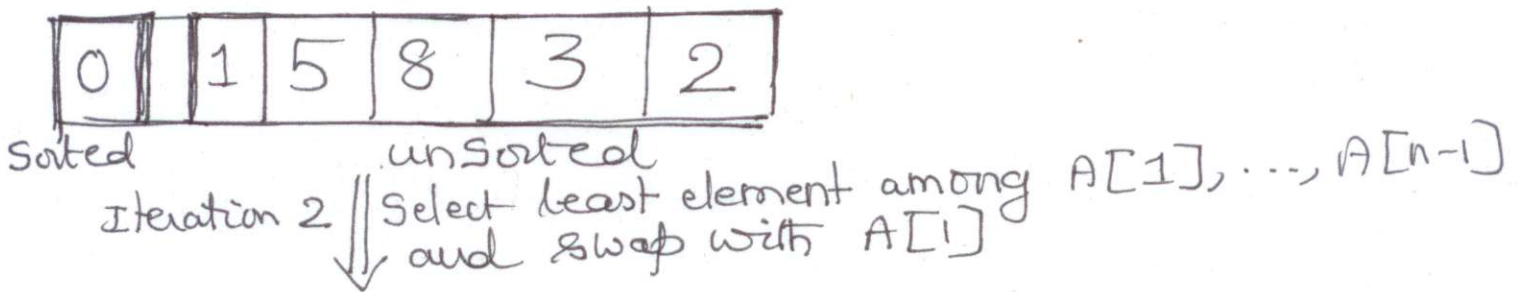
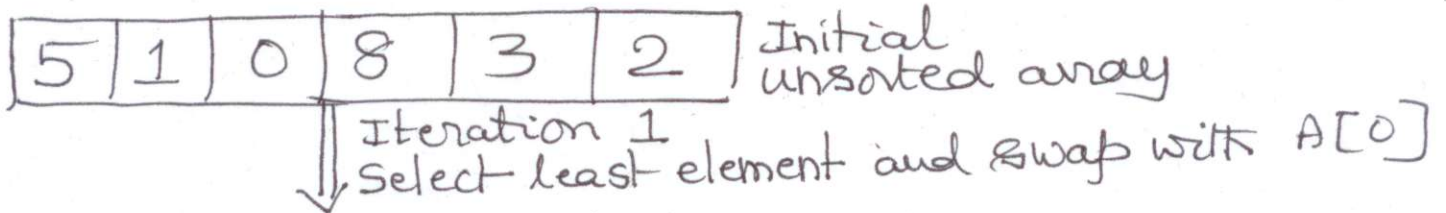


• Number of iterations = $n-1$

Number of	Minimum	Maximum
Comparisons	$\frac{n(n-1)}{2}$	$\frac{n(n-1)}{2}$
Exchanges	0 (happens for sorted input array)	$\frac{n(n-1)}{2}$

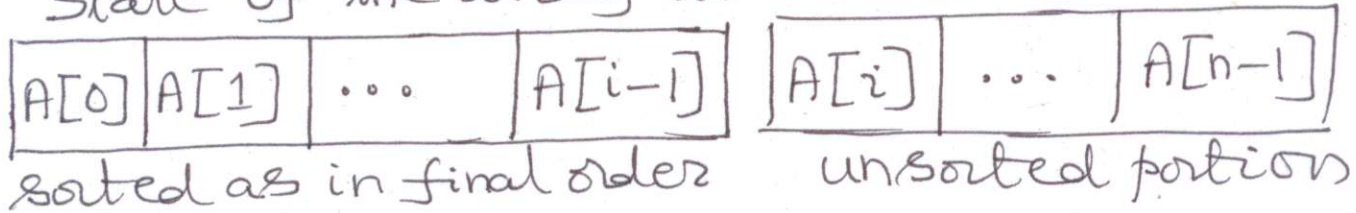
SELECTION SORT

In each iteration, the smallest element in the unsorted portion is "selected" and exchanged with the appropriate element. An example follows.

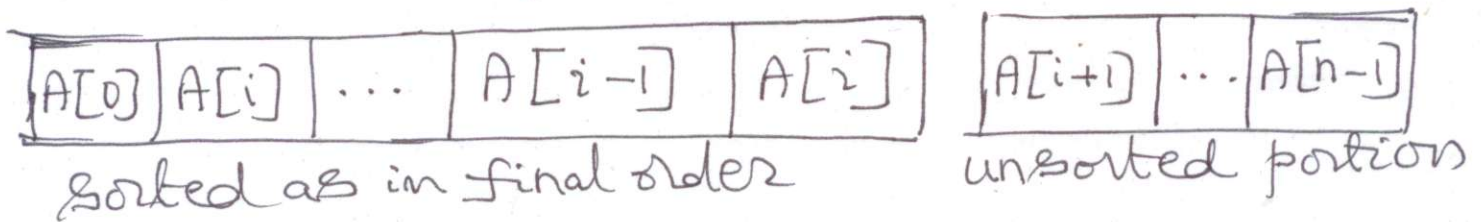


Summary of Selection Sort

State of the array at the end of iteration " i "



iteration ($i+1$)
 ↓
 "select" the minimum element in
 the unsorted portion and
 exchange it with $A[i]$

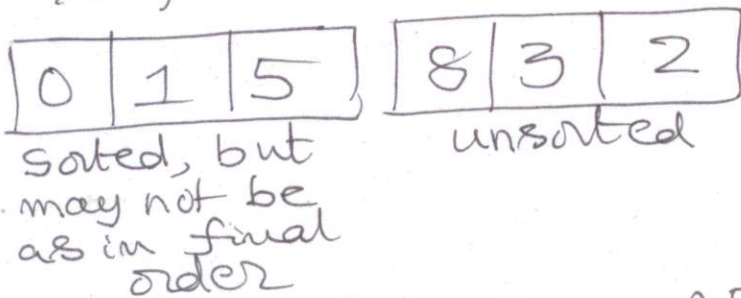
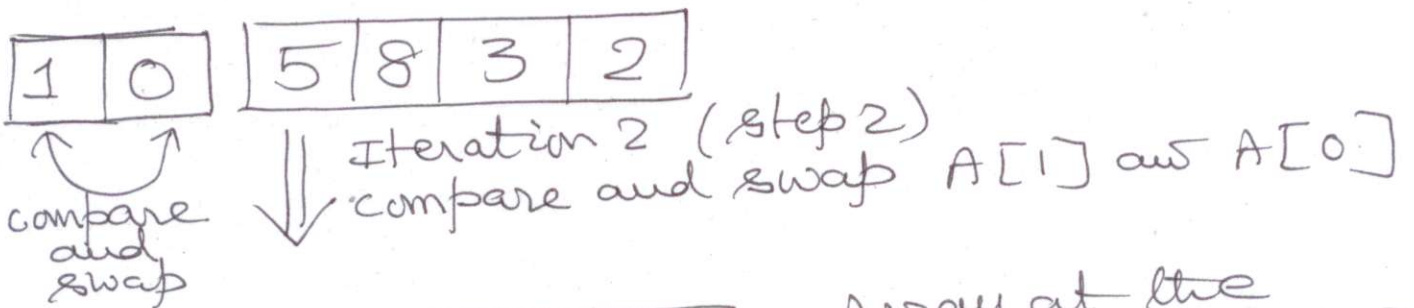
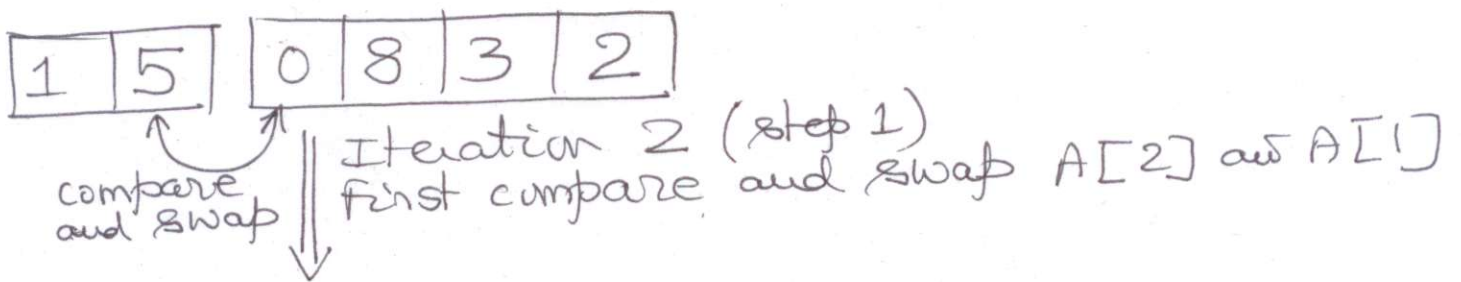
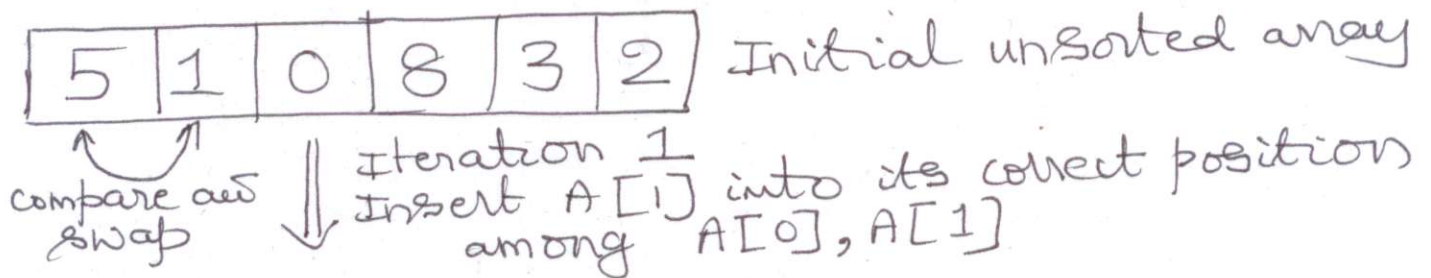


Number of iterations = $n-1$

Number of	Minimum	Maximum
Comparisons	$\frac{n(n-1)}{2}$	$\frac{n(n-1)}{2}$
Exchanges	$(n-1)$ (can be made zero at the cost of an additional $(n-1)$ comparisons)	$(n-1)$

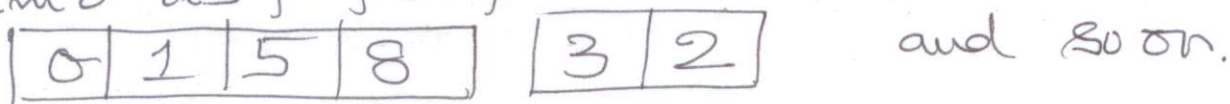
INSERTION SORT

In this method, there are $(n-1)$ iterations. At the end of iteration $(i-1)$, the elements $A[0], \dots, A[i-1]$ would be in ascending order. During iteration " i ", the element $A[i]$ is inserted into its correct position among $A[0], \dots, A[i-1]$ through a series of comparisons and exchanges. An example:



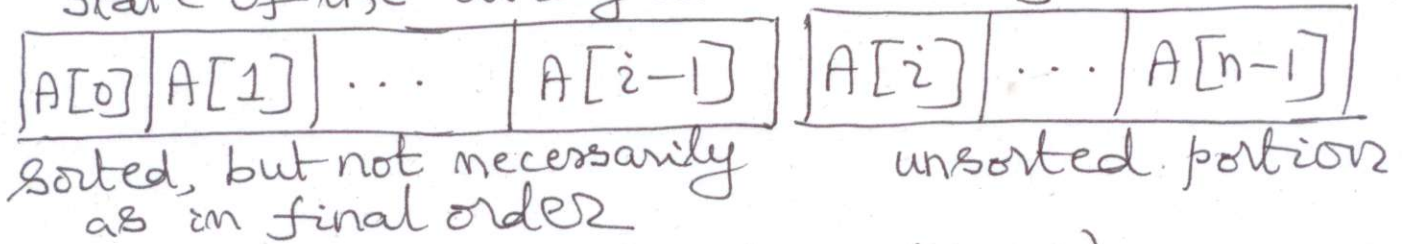
Array at the end of iteration 2

During iteration 3, $A[3]$ would be inserted into its proper position and we obtain



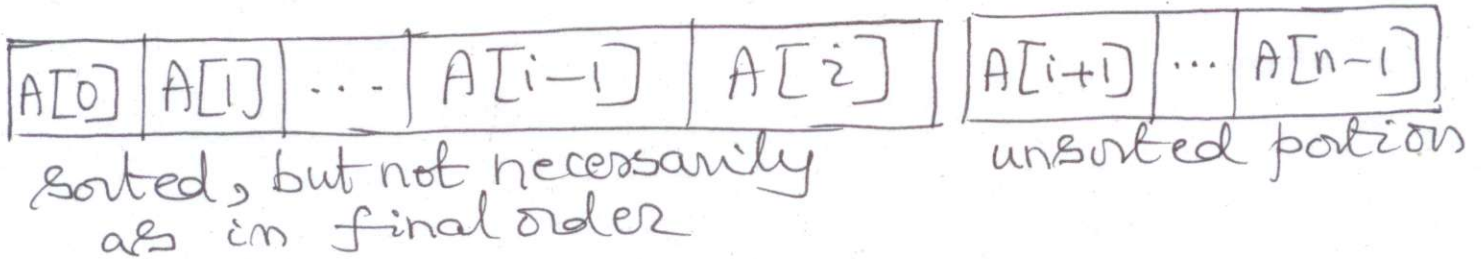
Summary of Insertion Sort

State of the array at the end of iteration " $i-1$ "



iteration (~~i~~)
 Insert $A[i]$ in the correct position among $A[0], \dots, A[i-1]$ through a series of exchanges

↓



Number of iterations = $n-1$

Number of	minimum	maximum
comparisons	$n-1$ (if the input array is already sorted)	$\frac{n(n-1)}{2}$
exchanges	0 (if the input array is already sorted)	$\frac{n(n-1)}{2}$